

# Dynamic Bond Portfolio Choice with Macroeconomic Information

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- Motivation and Related Literature

# Outline

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- Portfolio choice of multi-period risk-averse investor includes a hedging demand component in addition to the myopic one à la Markowitz
- Hedging demand arises due to investor's desire to hedge against adverse shocks to the underlying state variables
- This issue becomes particularly important if returns are predictable

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- But evidence on stock returns' predictability is rather weak (e.g. Goyal and Welch, 2008)
- On the other hand, bond yields are more reliably predictable by macroeconomic variables (Ang and Piazzesi, 2003)

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- Theoretical treatment: Wachter (2003), Liu (2007)

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- Explicitly utilize macroeconomic information for asset allocation (neglected in the literature)
- There are 5 macroeconomic factors -> examine portfolio choice among multiple bonds with different maturities

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- Examine the diversification and hedging value of real bonds for a multi-period risk-averse investor
- Evaluate the term structure model of Dewachter et al. (2006) from an asset allocation perspective

- Setup of Dewachter et al. (2006): 5 stochastically time-varying risk factors: output gap  $y$ , inflation rate  $\pi$ , real interest rate  $\rho$ , inflation central tendency  $\pi^*$  and central tendency of real interest rate  $\rho^*$ . Dynamics given by the following SDEs:

$$\begin{aligned}dy &= [\kappa_{yy}y + \kappa_{y\pi}(\pi - \pi^*) + \kappa_{y\rho}(\rho - \rho^*)]dt + \sigma_y dw_y \\d\pi &= [\kappa_{\pi y}y + \kappa_{\pi\pi}(\pi - \pi^*) + \kappa_{\pi\rho}(\rho - \rho^*)]dt + \sigma_\pi dw_\pi \\d\rho &= [\kappa_{\rho y}y + \kappa_{\rho\pi}(\pi - \pi^*) + \kappa_{\rho\rho}(\rho - \rho^*)]dt + \sigma_\rho dw_\rho \\d\pi^* &= \kappa_{\pi^*\pi^*}(\pi^* - \theta_{\pi^*})dt + \sigma_{\pi^*} dw_{\pi^*} \\d\rho^* &= \kappa_{\rho^*\rho^*}(\rho^* - \theta_{\rho^*})dt + \sigma_{\rho^*} dw_{\rho^*}\end{aligned}$$

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- Collect them in  $X = (y, \pi, \rho, \pi^*, \rho^*)$ :

$$dX = [\bar{\psi} + KX]dt + Sdw$$

# Bond returns dynamics

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- The price of a zero-coupon default-free nominal bond at time  $t$  maturing at time  $t + \tau \equiv T$  is given by:

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- No-arbitrage pricing dictates that returns' dynamics of the zero-coupon bond  $i$  are given by:

$$\frac{dP_i}{P_i} = (r - b(\tau)^T S^2 \Lambda - b(\tau)^T \Xi X) dt - b(\tau)^T S dw$$

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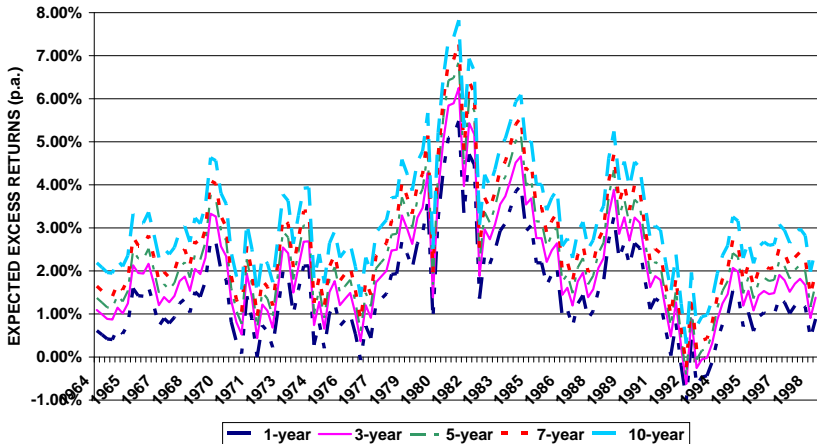
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- Filtered series: inflation central tendency exhibits very low volatility and it is highly persistent

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- Central tendency of inflation has a dominant impact on bonds' yields for longer than 2-y maturities (similar to a "level" factor)
- Filtered series: inflation central tendency exhibits very low volatility and it is highly persistent
- Considerable time-variation + strong co-movement in bonds' expected returns (mainly via inflation central tendency). "Reasonable" premia wrt previous studies (e.g. Sangvinatsos and Wachter, 2005)

# Bonds' expected excess returns

EXPECTED EXCESS RETURNS OF NOMINAL BONDS UNDER THE NOMINAL SDF



# Bond returns' covariance and correlation structure

**Panel A: Covariance Matrix**

	1-year	2-year	3-year	5-year	7-year	10-year
1-year	0.0004					
2-year	0.0007	0.0014				
3-year	0.0009	0.0019	0.0026			
5-year	0.0013	0.0026	0.0037	0.0054		
7-year	0.0016	0.0032	0.0046	0.0069	0.0088	
10-year	0.0019	0.0041	0.0058	0.0058	0.0115	0.0153

**Panel B: Correlation Matrix**

	1-year	2-year	3-year	5-year	7-year	10-year
1-year	1					
2-year	0.974	1				
3-year	0.947	0.994	1			
5-year	0.897	0.964	0.987	1		
7-year	0.848	0.927	0.961	0.993	1	
10-year	0.782	0.871	0.916	0.968	0.991	1

- Very low variances at short maturities -> Very high Sharpe ratios.  
Extremely high correlation for near maturities.

# Intertemporal portfolio choice

- Use the martingale methodology (Cox and Huang, 1989) to solve the intertemporal portfolio choice problem. The long-term investor maximizes power utility over REAL terminal wealth:

$$\max E_{t_0} \left\{ \frac{\left(\frac{W_T}{\Pi_T}\right)^{1-\gamma}}{1-\gamma} \right\}, \quad 0 < \gamma \neq 1$$

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- Dynamics for price level process  $\Pi$ :

$$\frac{d\Pi}{\Pi} = \pi dt + \sigma_{\Pi}^T dw$$

# Calculating the optimal portfolio

- Subject to conditions, optimal portfolio choice is given by:

$$\begin{aligned}\phi_t = & \frac{1}{\gamma}(B^T S^2 B)^{-1}(-B^T S^2 \Lambda - B^T \Xi X_t) \\ & + (1 - \frac{1}{\gamma})(B^T S^2 B)^{-1}(-B^T S)\sigma_{\Pi} \\ & + \frac{1}{\gamma}(B^T S^2 B)^{-1}(-B^T S)S[d(t) + \frac{1}{2}(Q(t) + Q(t)^T)X_t]\end{aligned}$$

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with  $d(t)$  and  $Q(t)$  satisfying a system of ODEs

- The remainder  $\phi_0 = 1 - i^T \phi$  is invested in the nominal instantaneously riskless asset yielding the risk-free rate  $r$

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- 2 interesting observations:
  - 1 Hedging demand depends on the diffusion coeff of risk factors' dynamics as well as the sensitivity of investor's wealth to the risk factors, represented by  $d(t)$  and  $Q(t)$ .
  - 2 Both myopic and hedging bond demands induce market timing, i.e. portfolio choice depends on the current level of risk factors.

# Incomplete markets

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- Methodological note: Incompleteness in our setup arises only due to the number of bonds
- When no. bonds = no. risk factors  $\rightarrow$  complete markets because inflation is an explicit risk factor (so shocks to price level process  $\Pi$  can be hedged too)

# Introducing real bonds

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- Returns' dynamics of real zero-coupon bond  $i$  given by:

$$\frac{dP_i^R}{P_i^R} = (r - \pi + \sigma_{\Pi}^T \xi - b^R(\tau)^T S \xi + b^R(\tau)^T S \sigma_{\Pi}) dt - b^R(\tau)^T S dw$$

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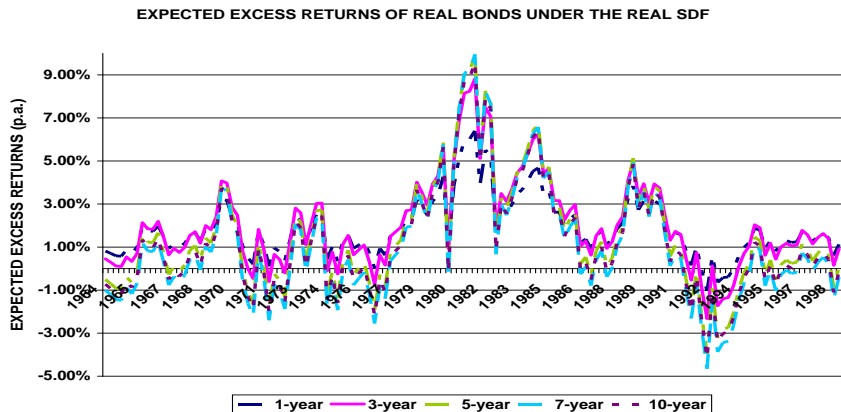
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- Intertemporal portfolio choice problem among real or among nominal+ real bonds solved using the same techniques



# Real bonds' excess returns



- Real bonds' excess returns turn negative (puzzling for myopic risk-averse investor). Significant time-variation+ strong co-movement

# Portfolio choice among two nominal bonds

**Panel A: Benchmark case 1975:Q1**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=3	T=5	T=10	T=0	T=3	T=5	T=10
3-yr	0.65%	0.05	5.17	4.66	1.94	0.03	3.79	3.88	2.01
10-yr	1.71%	0.26	0.29	1.28	3.12	0.10	0.02	0.63	2.12

**Panel B: One St. dev. increase in inflation central tendency**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=3	T=5	T=10	T=0	T=3	T=5	T=10
3-yr	0.88%	0.84	9.39	8.77	5.47	0.35	6.07	6.13	3.82
10-yr	1.96%	0.002	-0.24	0.94	3.15	-0.004	-0.23	0.52	2.32

**Panel C: One St. dev. decrease in inflation central tendency**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=3	T=5	T=10	T=0	T=3	T=5	T=10
3-yr	0.42%	-0.74	0.94	0.56	-1.59	-0.28	1.52	1.64	0.19
10-yr	1.46%	0.52	0.82	1.62	3.09	0.20	0.26	0.74	1.91

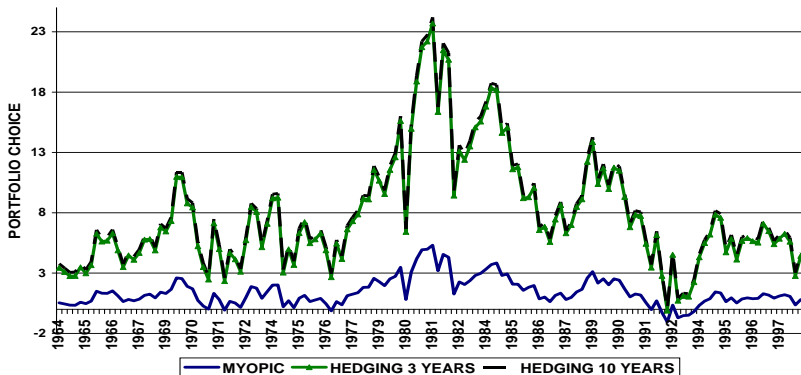
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- Shifts in the macroeconomy (in particular inflation central tendency) affect bonds' premia and hence change myopic and hedging demands
- Allocation among bonds changes with investment horizon- investor attempts to combine bonds' maturities so as to match his investment horizon+ hedge shocks to his real wealth process

# Sensitivity analysis (2 bonds, RRA=10, T=3 and 10 years)

TOTAL MYOPIC AND HEDGING DEMANDS FOR 2 NOMINAL BONDS



- Implausibly high myopic and hedging demands due to high Sharpe ratios and extremely low variances of risk factors

# Portfolio choice among three bonds

**Panel A: Three nominal bonds (nominal SDF) 1975:Q1**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=1	T=5	T=10	T=0	T=1	T=5	T=10
1-yr (N)	0.20%	1.74	0.73	-5.96	-3.89	0.14	-0.25	-5.77	-4.31
5-yr (N)	0.91%	-1.61	1.27	8.66	4.09	-0.27	1.53	8.08	4.74
10-yr (N)	1.71%	0.99	-0.07	-1.07	2.13	0.25	-0.42	-1.66	0.91

**Panel B: Three real bonds (real SDF) 1975:Q1**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=1	T=5	T=10	T=0	T=1	T=5	T=10
1-yr (R)	0.34%	29.69	31.68	30.51	31.71	11.87	13.42	12.52	13.40
5-yr (R)	-1.37%	-12.96	-13.45	-15.90	-20.92	-5.18	-5.44	-6.64	-10.67
10-yr (R)	-1.59%	3.83	4.47	9.46	13.76	1.53	1.87	5.13	8.78

**Panel C: Three nominal and real bonds under the nominal SDF 1975:Q1**

	Premia	$\gamma=4$				$\gamma=10$			
		T=0	T=1	T=5	T=10	T=0	T=1	T=5	T=10
1-yr (N)	0.20%	2.98	4.71	4.81	2.28	0.87	2.00	1.99	1.17
5-yr (R)	-0.84%	-1.42	-0.99	0.83	-0.37	-0.46	-0.14	1.08	0.63
10-yr (N)	1.71%	0.60	0.63	3.15	3.74	0.23	0.23	1.30	2.43

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- Investor again combines bonds' maturities so as to match his horizon
- Real bonds useful for both diversification (lower correlation with nominal bonds) and hedging (better hedge against shocks to real wealth process)
- For the infinitely long-term risk averse investor with utility over real terminal wealth, the only *risk-free* asset is the zero-coupon bond whose maturity *matches* his horizon

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- Serious failure from an asset allocation perspective because they imply extremely high risky assets' demands
- Parameter uncertainty potential way out
- Failure of the expectation hypothesis induces considerable market timing for a myopic investor  
+ great hedging demands for a multi-period risk averse investor
- Macroeconomic information particularly important for bond investors  
-> incorporate it in portfolio choice context (e.g. the life-cycle model of Koijen et al. (2009))

Thank you for attending!

